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Summary

- The statistics and graphics features of R are easily accessible from APL+Win using the `□cse` system function and the R.Net interface to R.

- What is R?

R is a statistics and graphics toolkit. Its origin is the S language developed at Bell Laboratories. R provides a wide variety of statistics and graphics tools. R is available as no-cost, open source software under the terms of the Free Software Foundation's GNU General Public License. R is in wide use by many enterprises both public and private.

- What is R.Net?

R.NET is a .Net interface to the R toolkit. R.Net is composed of .Net assemblies which enable programs written using a .NET Framework programming language, e.g. C#, to collaborate with the R toolkit. R.Net is available as no-cost, open source software under the terms of its BSD license.

- What is the APL+Win CSE?

The APL+Win `□cse` system function is an interface to the APLNext C# Script Engine (CSE). Using the `□cse` system function, APL+Win can execute CSE scripts, employing the R.Net assemblies, to use the R toolkit.

- Why interface APL+Win and R?

Certainly any feature of R could be duplicated in APL+Win, assuming that the appropriate time and technical expertise are available to implement the required feature. R is used by many scientific, research and commercial entities worldwide so it incorporates tested tools for statistics and graphics. From the economic and practical points-of-view, using R for what it can do is a rational decision.

Prerequisites

To run the examples in this document the following components must be installed on the target workstation:

- APL+Win version 14.0.04+, available from [APL2000](#), has its own installer.
- Microsoft .Net Framework 4.5, [available from Microsoft](#) at no cost, has its own installer.
- The APLNext C# Script Engine v1.0.102+ (CSE), included in the [APL+Win subscription](#), has its own installer which should be 'run as administrator'.

- R toolkit, available from many sources (e.g. [US NIH](#)), has its own installer which should be 'run as administrator'. Review the [installation instructions](#) and the [R FAQ](#) for this component. The physical path at which the 32-bit version of the R toolkit has been installed is required to run the examples in this document.
- The .Net assemblies (RDotnet.dll and RDotNet.NativeLibrary.dll) for the R.Net R toolkit which are included in the .zip file containing this document or can be obtained from the [R.Net project website](#). It may be necessary to 'Unblock' these assemblies in their Windows Explorer Properties dialog so that they can be loaded by the CSE.
- The APL+Win 'R Stat&Graph.w3' workspace, which accompanies this document, contains the APL+Win functions used in the examples.

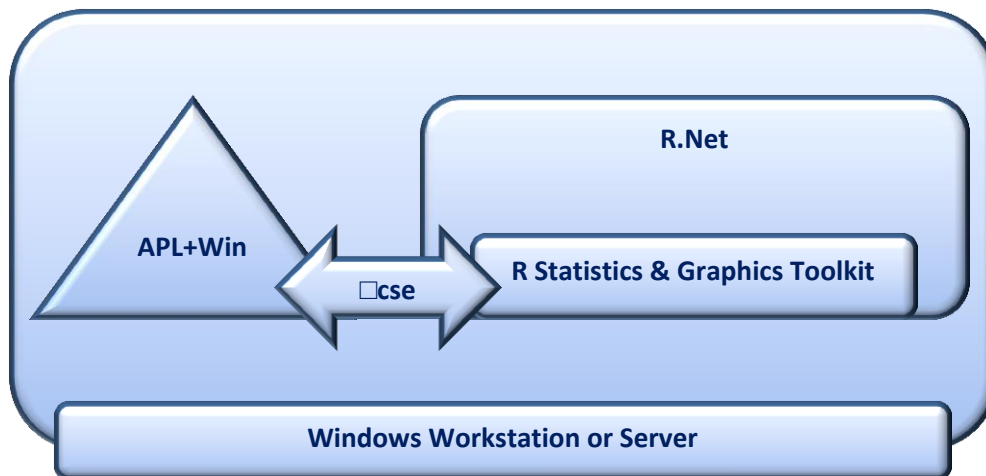
After the above components are installed:

- The examples in this document can be run starting from an APL+Win programmer session.
- The examples in this document are for demonstration purposes only.
- The examples use specific versions of R and R.Net, so modifications to the APL+Win functions may be necessary if subsequent versions of these components are used.

- The location of the APL+Win interpreter executable and the R.Net assemblies using for the examples may need to be modified for your environment. The examples assume that the current folder, i.e. `□chdir`”, contains the required components.
- In the current implementation of R only one instance of the R engine can be created by an application during an application session.
- To run the examples in this document it is necessary create an instance of the R engine at the start of the APL+Win session (by running the APL+Win ‘InitREngine’ function) and close it at the end of the APL+Win session (by running the APL+Win ‘CloseREngine’ function).

Object Model of APL+Win and the R Statistics & Graphics Toolkit

R.Net is a .Net (C#) interface to the R Statistics and Graphics toolkit. From APL+Win the `□cse` system function creates an instance of the R.Net object so that APL+Win can use the R toolkit with an object-oriented object model.



Shared APL+Win Functions Used in the Examples

To initialize an instance of the CSE (with `□cself` set to 'RNet') and create an instance of the R.Net engine (called 'rEng'), the APL+Win 'InitREngine' function is used. The installation path of the R software is required in this function and the R.Net assemblies are assumed to be in the current folder. The default installation path of the R software is illustrated.

```
InitREngine;sink
```

```
:TRY *
```

```
□ cself ← 'RNet'
```

```
sink ← □ cself □ cse 'Init' 'System'
```

```
sink ← □ cse 'ExecStmt' 'using System;'
```

```
sink ← □ cse 'returnonerror' 1
```

⌚ ↑ Express C# exceptions as APL+Win exceptions

```
sink ← □ cse 'LoadAssemblyByName' 'System.Core'
```

```
sink ← □ cse 'LoadAssemblyByName' 'System.Data'
```

```
sink ← □ cse 'LoadAssemblyByName' 'System.Data.DataSetExtensions'
```

```
sink ← □ cse 'LoadAssemblyByName' 'System.Numerics'
```

```
sink ← □ cse 'LoadAssemblyByName' 'System.Xml'
```

```
sink ← □ cse 'LoadAssemblyByName' 'System.Xml.Linq'
```

```
sink ← □ cse 'LoadAssembly' 'RDotNet.dll'
```

```
sink ← □ cse 'LoadAssembly' 'RDotNet.NativeLibrary.dll'
```

⌚ ↑ .Net assemblies required for this project

⌚ ↑ They are assumed to be in the current folder

- ⌚ Alternatively they could be put into the .Net GAC
- ⌚ and loaded with the `LoadAssemblyByName` method

```
sink←□cse 'ExecStmt' 'using System.Collections.Generic;'
```

```
sink←□cse 'ExecStmt' 'using System.Linq;'
```

```
sink←□cse 'ExecStmt' 'using System.Text;'
```

```
sink←□cse 'ExecStmt' 'using System.IO;'
```

```
sink←□cse 'ExecStmt' 'using System.Data;'
```

```
sink←□cse 'ExecStmt' 'using RDotNet;'
```

- ⌚ ↑Establish namespace shortcuts

```
sink←□cse 'ExecStmt' 'var envPath =  
Environment.GetEnvironmentVariable("PATH");'
```

```
sink←□cse 'ExecStmt' 'string rBinPath = @"C:\Program Files\R\R-  
3.0.2\bin\i386";'
```

```
sink←□cse 'ExecStmt' 'Environment.SetEnvironmentVariable("PATH",  
envPath + Path.PathSeparator + rBinPath);'
```

- ⌚ ↑Requires elevated priviledges

⌚ ↑R requires that a Win OS Path be defined

⌚ ↑X86 version selected so that R can be used from APL+Win (Win32)

```
sink←⎕cse 'ExecStmt' 'REngine rEng =REngine.CreateInstance("APLNextR");'
```

```
sink←⎕cse 'ExecStmt' 'rEng.Initialize()';'
```

⌚ ↑Create an instance of RDOTNOT.REngine class called rEng

```
:CATCHALL
```

```
⎕error ('InitREngine failed: ',⎕dm)
```

```
:ENDTRY
```

To close the R.Net engine instance and the CSE instance, the APL+Win 'CloseEngine' function is used.

```
CloseEngine;sink
:TRY
:IF 0<1↑ρ⊞cself ⊞cse 'self'
  sink←⊞cse 'ExecStmt' 'rEng.Close();'
  sink←'C' ⊞cse 'Close'
:ENDIF
:CATCHALL
:ENDTRY
```


Creating, Saving and Displaying an R-plot in APL+Win

This example illustrates saving an R-plot to an image file in the bitmap format and displaying that image on an APL+Win `□wi` form. Run the APL+Win `'ShowRPlotInAPLWinForm'` function to see the results. This function uses the REngine instance to create an R-plot of the Gauss probability density as a bitmap file and uses that bitmap file to display the R-plot image in an APL+Win form.

Instead of directly computing the Gauss probability density function for a selection of values and using the R `'plot()'` function, it would also be possible to use the R-function `'rnorm(#vals, mean, stddev)'` to generate samples of a Gauss-distributed random variable and then use the R `'hist()'` function to generate a similar chart.

```
ShowRPlotInAPLWinForm;F;P;sink
```

```
⌈⌋APLNext 20131229
```

```
:TRY *
```

```
sink←⌈⌋cse 'ExecStmt' 'double[] x = new double[200];'
```

```
sink←⌈⌋cse 'SetValue' 'x' (0.04×(1200)-100)
```

```
⌈⌋ ↑ Create x-axis elements for the plot using APL+Win
```

```
⌈⌋ ↑ Set the value of the C# variable 'x' from APL+Win
```

```
sink←⌈⌋cse 'ExecStmt' 'rEng.SetSymbol("x", rEng.CreateNumericVector(x));'
```

```
⌈⌋ ↑ Set R symbol "x"
```

```
sink←⌈⌋cse 'ExecStmt' 'rEng.Evaluate("@y <- 1/sqrt(2*pi)*exp(-x^2/2)");'
```

```
⌈⌋ ↑ Using R, compute the Gauss probability density function for each x-axis element
```

```
⌈⌋ and assign the results to y
```

```
sink←⌈⌋cse 'ExecStmt' 'string chartFnm = @"chartFnm.bmp";'
```

```
sink←⌈⌋cse 'ExecStmt' 'File.Delete(chartFnm);'
```

```

sink←□cse 'ExecStmt'
'rEng.SetSymbol("chartFnm",rEng.CreateCharacterVector(new
string[]{chartFnm}));'
sink←□cse 'ExecStmt' 'rEng.Evaluate("bmp(chartFnm)");'
⌕ ↑Set the saved chart bitmap destination

sink←□cse 'ExecStmt' 'rEng.Evaluate("@plot(x,y,type=""l'");'
⌕ ↑Create the line plot using R
sink←□cse 'ExecStmt' 'rEng.Evaluate("@dev.off()");'
⌕ ↑Write the chart to the target bitmap file

F←'F'□wi 'Create' 'Form' ('size' 40 80) ('caption' 'R-plot in APL+Win Form')
P←'F.P'□wi 'Create' 'Picture' ('where' 0 0 40 80) ('imagesize' 38 78) ('style' 4)
P□wi 'bitmap' 'chartFnm.bmp'
sink←F□wi 'Wait'
⌕ ↑Display the chart in a modal APL+Win form

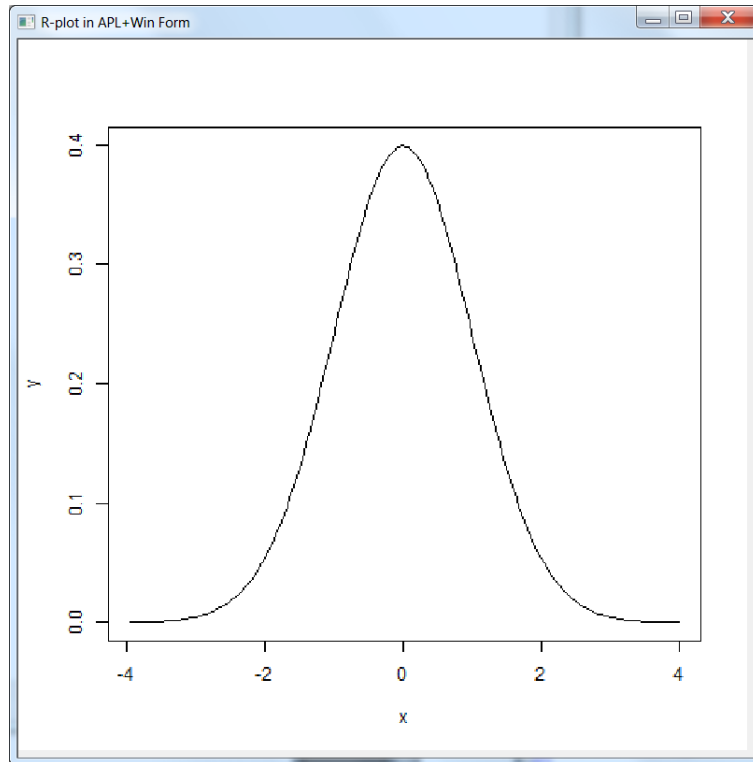
:CATCH

```

'ShowRPlotInAPLWinForm failed: ', ☐ dm

:ENDTRY

To keep this example simple, the format of the illustrated plot is elementary. With some study of the R documentation for plotting and graphics much more sophisticated charts can be prepared.



R-Plot illustrating the Central Limit Theorem

In this example two R-plots are placed in the same chart. The first is a histogram of sample averages and the second is a line chart of the same averages to illustrate the anticipated effect of the Central Limit Theorem.

CentralLimitChart;F;P;sink;trialVals

⌕ APLNext 20140222

:TRY *

sink←□cse 'ExecStmt' 'string chartFnm = @"chartFnm.bmp";'

sink←□cse 'ExecStmt' 'File.Delete(chartFnm);'

sink←□cse 'ExecStmt'

'rEng.SetSymbol("chartFnm",rEng.CreateCharacterVector(new
string[] {chartFnm}));'

sink←□cse 'ExecStmt' 'rEng.Evaluate("bmp(chartFnm)");'

⌕ ↑Set the saved chart bitmap destination

trialVals←1E⁻⁴×16 1000ρ?“(×/16 1000)ρ×/16 1000

⌕ ↑In a production environment, trialVals would come from a simulation or
other experiment involving trials of a model

sink←□cse 'ExecStmt' 'double[,] trialVals = new double[16,1000];'

⌕ ↑Create C# matrix to receive APL+Win values

sink←□cse 'SetValue' 'trialVals' trialVals

⌚ ↑Set C# matrix with the APL+Win values

```
sink←□cse 'ExecStmt' 'var rmt = rEng.CreateNumericMatrix(trialVals);'
```

⌚ ↑Create an R.Net variable containing the APL+Win values

```
sink←□cse 'ExecStmt' 'rEng.SetSymbol("rmt",rmt);'
```

⌚ ↑Create a R symbol containing the APL+Win values

```
sink←□cse 'ExecStmt' 'rEng.Evaluate(@"mns <- cbind(rmt[ 1, ],apply(rmt[ 1:4,  
], 2, mean),apply(rmt[ 1:16, ], 2, mean))");'
```

⌚ ↑Compute the means of samples of 1, 4, 16

```
sink←□cse 'ExecStmt' 'rEng.Evaluate(@"meds <- cbind(rmt[ 1, ],apply(rmt[  
1:4, ], 2, median),apply(rmt[ 1:16, ], 2, median))");'
```

⌚ ↑Compute the medians of samples of 1, 4, 16

```
sink←□cse 'ExecStmt' 'rEng.Evaluate(@"hist(mns[,3], main = ""Means of  
samples of size 16"",xlab = ""Size 16 means"", las = 1, col = ""darkred"", breaks  
= 50, prob = TRUE)");'
```

```
sink←□cse 'ExecStmt' 'rEng.Evaluate(@"lines(density(mns[,3]), col =  
""blue"");'
```

⌚ ↑Define the R-plot type, axis labels, colors, etc.


```
sink←□cse 'ExecStmt' 'rEng.Evaluate(@"dev.off()");'
```

⌚ ↑Write the chart to the target bitmap file

```
F←'F'□wi 'Create' 'Form' ('size' 40 80) ('caption' 'R-plot in APL+Win Form')
```

```
P←'F.P'□wi 'Create' 'Picture' ('where' 0 0 40 80) ('size' 30 60) ('style' 0)
```

```
P□wi 'bitmap' 'chartFnm.bmp'
```

```
sink←F□wi 'Wait'
```

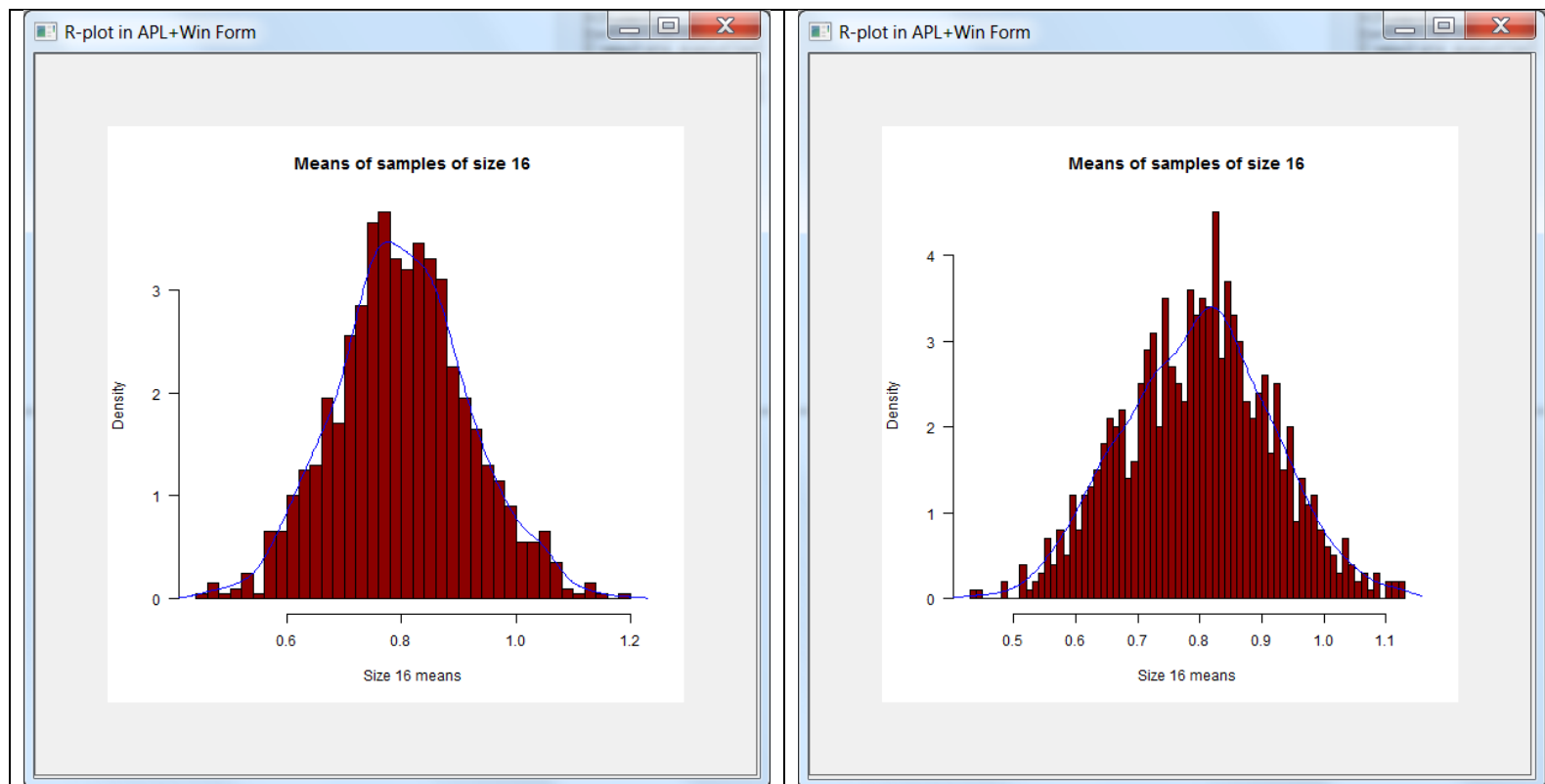
⌚ ↑Display the chart in a modal APL+Win form

```
:CATCH
```

```
'CentralLimitChart failed: ',□dm
```

```
:ENDTRY
```

When the APL+Win 'CentralLimitChart' function is run, an APL+Win form is displayed containing the JPEG-format image containing the R-plot. Since the 'trial' data used in this example is based on the APL+Win 'deal' function, running this function a few times gives a graphic representation of the APL+Win random number generator results.



R-Plot of Beta Distribution

The beta distribution has two parameters α and β which provide flexibility to specify an asymmetrical probability distribution with mean $1+(1/(\beta/\alpha))$. The APL+Win 'BetaDistChart' function has a three element right argument (#values α β). This function uses the R-function 'rbeta(#vals, α , β)' to generate n sample values of a beta-distributed random variable and then plots these values using the R-function 'hist()'.

BetaDistChart X;F;P;sink;trialVals;n;a;b

⌈ APLNext 20140226

⌈ X[1]: #vals

⌈ X[2]: alpha

⌈ X[3]: beta

(n a b)←X

:TRY *

sink←□cse 'ExecStmt' 'string chartFnm = @"chartFnm.bmp";'

sink←□cse 'ExecStmt' 'File.Delete(chartFnm);'

sink←□cse 'ExecStmt'

'rEng.SetSymbol("chartFnm",rEng.CreateCharacterVector(new
string[] {chartFnm}));'

sink←□cse 'ExecStmt' 'rEng.Evaluate("bmp(chartFnm)");'

⌈ ↑Set the saved chart bitmap destination

sink←□cse 'ExecStmt' 'double[] n = new double[1];'

```
sink←□ cse 'SetValue' 'n[0]' n  
sink←□ cse 'ExecStmt' 'rEng.SetSymbol("n",rEng.CreateNumericVector(n));'
```

```
sink←□ cse 'ExecStmt' 'double[] a = new double[1];'  
sink←□ cse 'SetValue' 'a[0]' a  
sink←□ cse 'ExecStmt' 'rEng.SetSymbol("a",rEng.CreateNumericVector(a));'
```

```
sink←□ cse 'ExecStmt' 'double[] b = new double[1];'  
sink←□ cse 'SetValue' 'b[0]' b  
sink←□ cse 'ExecStmt' 'rEng.SetSymbol("b",rEng.CreateNumericVector(b));'
```

```
sink←□ cse 'ExecStmt' 'rEng.Evaluate(@"b <- rbeta(n,a,b)");'  
sink←□ cse 'ExecStmt' 'rEng.Evaluate(@"hist(b, prob = TRUE, breaks=50, col =  
""darkred""));'
```

⌚ ↑ Define the R-plot type, axis labels, colors, etc.

```
sink←□ cse 'ExecStmt' 'rEng.Evaluate(@"dev.off()");'
```

⌈ ↑ Write the chart to the target bitmap file

```
F←'F'⎕wi 'Create' 'Form' ('size' 40 80) ('caption' 'R-plot in APL+Win Form')
```

```
P←'F.P'⎕wi 'Create' 'Picture' ('where' 0 0 40 80) ('size' 30 60) ('style' 0)
```

```
P⎕wi 'bitmap' 'chartFnm.bmp'
```

```
sink←F⎕wi 'Wait'
```

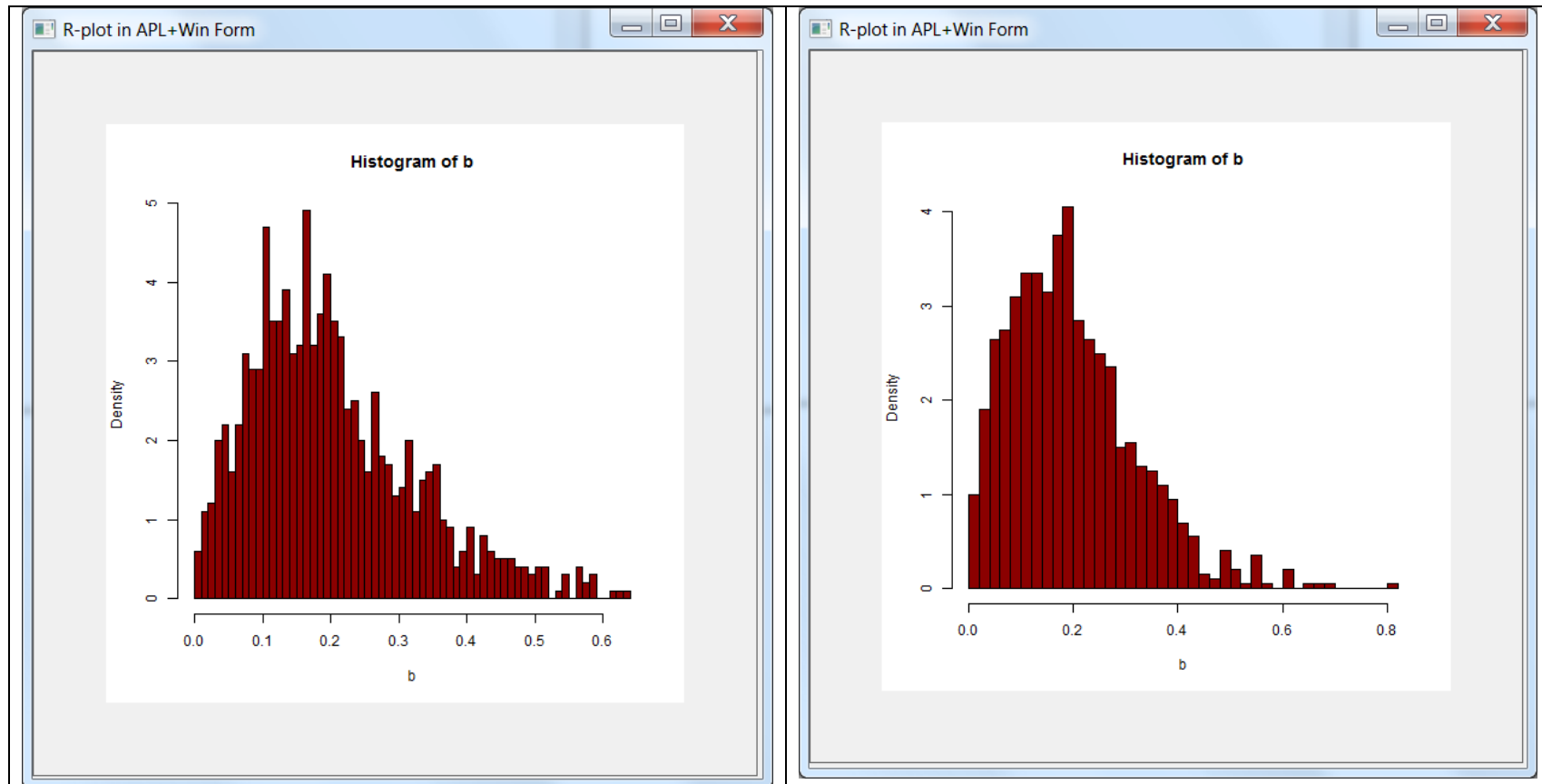
⌈ ↑ Display the chart in a modal APL+Win form

```
:CATCH
```

```
'CentralLimitChart failed: ',⎕dm
```

```
:ENDTRY
```

Sample R-plots (mean 0.2) using a right argument of 1000 2 8 for the APL+Win 'BetaDistChart' function.



Using R for *ad hoc* Calculations in APL+Win

This example illustrates creating an APL+Win GUI form application which requests user input, responds to the user's button click event and uses the R Engine to perform an *ad hoc* calculation. The APL+Win 'UseRToCalculateAdHoc' function defines the APL+Win GUI form with Edit controls for input and output Edit and a Button control, subscribed to the Button click event with the 'UseRToCalculateAdHocEH' function and waits for user input.

UseRToCalculateAdHoc;F;LI;EE;EI;BN;LO;EO;sink

⌕ APLNext 20131215

:TRY

```
F←'F'□wi 'Create' 'Form' ('size' 20 80) ('caption' 'Use R for ad hoc calculation')
LI←'F.LI'□wi 'Create' 'Label' ('where' 1 0) ('caption' 'Enter Radius: ')
EI←'F.EI'□wi 'Create' 'Edit' ('where' 1 20 2 20) ('text' '1')
BN←'F.BN'□wi 'Create' 'Button' ('where' 4 2 2 25) ('caption' 'Calculate using
APL+Win and R')
BN□wi 'onClick' 'UseRToCalculateAdHocEH'
LO←'F.LO'□wi 'Create' 'Label' ('where' 8 0) ('caption' 'Area of Circle: ')
EO←'F.EO'□wi 'Create' 'Edit' ('where' 8 20 2 20)
EE←'F.EE'□wi 'Create' 'Edit' ('where' 12 10 5 50) ('style' 4 16)
sink←F □wi 'Wait'
⌕ ↑Define an APL+Win GUI form, set the button click event handler, wait for
user
sink←F □wi 'Close'
```

```
:CATCHALL
```

```
'UseRToCalculateAdHoc failed: ', dm
```

```
:ENDTRY
```

The 'UseRToCalculateAdHocEH' event handler function obtains the user input, passes it to the R.Net engine instance, requests the calculation from the R Engine, gets the result into APL+Win and displays the result on the APL+Win GUI form.

UseRToCalculateAdHocEH;radius;area

⌕ APLNext 20131215

:TRY

'F.BN' ⌕ wi 'enabled' 0

⌕ ↑ Disable user input during event handler function execution

radius←1↑ ⌕ FI 'F.EI' ⌕ wi 'text'

⌕ ↑ Get the user input from the APL+WIN form

sink← ⌕ cse 'ExecStmt' 'double radius = 0;'

sink← ⌕ cse 'SetValue' 'radius' (1⊃radius,0.5)

⌕ ↑ Set C# input variable from the APL+Win variable coerced to double in APL+Win

sink← ⌕ cse 'ExecStmt' 'rEng.SetSymbol("radius",
rEng.CreateNumericVector(new double[] {radius}));'

⌕ ↑ Set R symbol "radius"

```
sink←□cse 'ExecStmt' 'rEng.Evaluate(@ "area <- pi*(radius^2)");'
```

⌚ ↑Using R, compute the area of the circle and assign the value to the R-symbol "area"

```
area←□cse 'GetValue' 'rEng.GetSymbol("area").AsNumeric().First()'
```

⌚ ↑Get the result from R

```
'F.EO'□wi 'text' (⌘ area)
```

⌚ ↑Display result in APL+Win form

```
:CATCH
```

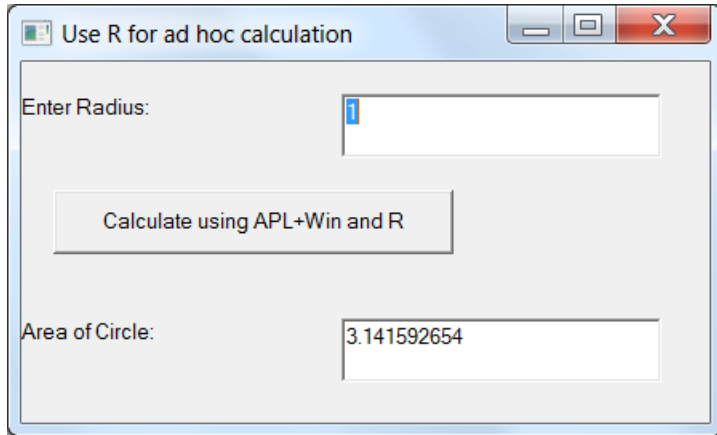
```
'F.EE'□wi 'text' ('Error: ',□dm)
```

```
:FINALLY
```

```
'F.BN'□wi 'enabled' 1
```

```
:ENDTRY
```

After the 'UseRToCalculateAdHoc' function is run, the user enters a radius value and clicks the 'Calculate...' button:



The screenshot shows a Windows-style application window titled "Use R for ad hoc calculation". Inside the window, there is a label "Enter Radius:" followed by a text input field containing the number "1". Below this is a button labeled "Calculate using APL+Win and R". At the bottom, there is a label "Area of Circle:" followed by a text output field displaying the value "3.141592654".

Creating and Executing a user-defined function in R with a scalar argument and result

Sometimes it is convenient to create a user-defined function in R so that it can be executed several times during the APL+Win session.

- Use the R.Net engine to evaluate a valid R function definition and cast it as an R.Net 'Function'
- Create the arguments for the function as an R.Net 'SymbolicExpression[]'
- Use the R.Net 'Invoke' method to execute the R.Net function

RUserDefinedFunction

☐ cse 'ExecStmt' 'var Add_10 = rEng.Evaluate(@"Add_10 <-function(x){x = x + 10;return(x);}").AsFunction();'

☐ cse 'ExecStmt' 'var l = rEng.CreateIntegerVector(new Int32[] { 100 });'

☐ cse 'ExecStmt' 'var se = new SymbolicExpression[] { l };'

☐ cse 'ExecStmt' 'var res = Add_10.Invoke(se).AsInteger();'

☐ cse 'ExecStmt' 'Int32 r = res.First();'

☐ cse 'GetValue' 'r'

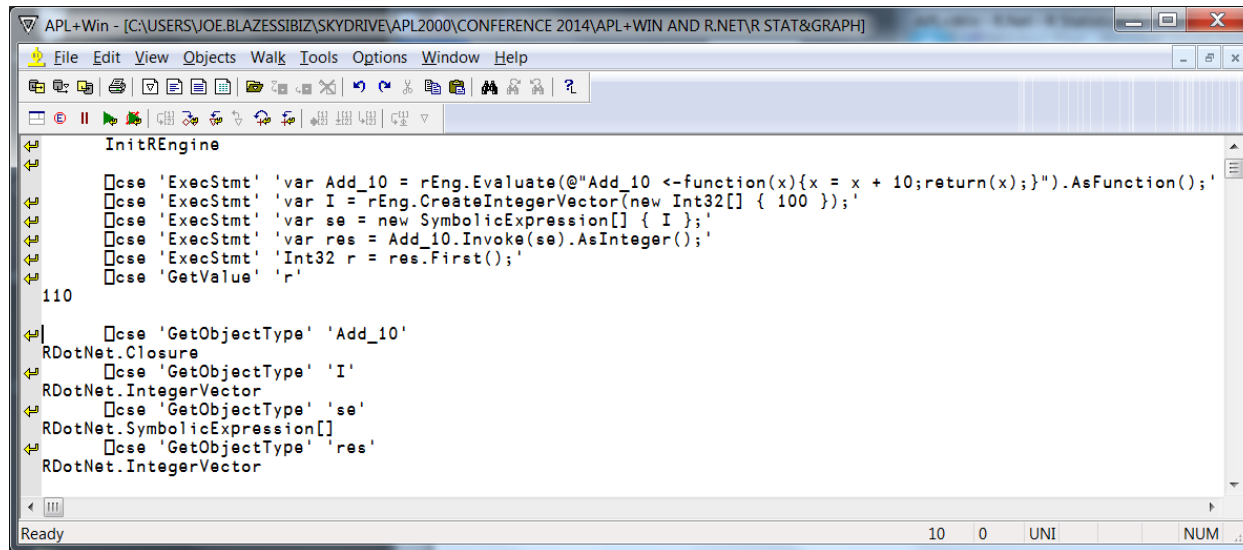
☐ cse 'GetObjectType' 'Add_10'

☐ cse 'GetObjectType' 'l'

☐ cse 'GetType' 'se'

☐ cse 'GetType' 'res'

When the APL+Win 'RUserDefinedFunction' function is run the 'Add_10 (100)' R-function is executed and the result captured in APL+Win.



The screenshot shows the APL+Win application window with the following content:

```
APL+Win - [C:\USERS\JOE.BLAZESSIBIZ\SKYDRIVE\APL2000\CONFERENCE 2014\APL+WIN AND R.NET\R STAT&GRAPH]
File Edit View Objects Walk Tools Options Window Help
[Icons]
InitREngine
  [cse 'ExecStmt' 'var Add_10 = rEng.Evaluate(@"Add_10 <-function(x){x = x + 10;return(x);}").AsFunction();'
  [cse 'ExecStmt' 'var I = rEng.CreateIntegerVector(new Int32[] { 100 });'
  [cse 'ExecStmt' 'var se = new SymbolicExpression[] { I };'
  [cse 'ExecStmt' 'var res = Add_10.Invoke(se).AsInteger();'
  [cse 'ExecStmt' 'Int32 r = res.First();'
  [cse 'GetValue' 'r'
110
  [cse 'GetObjectType' 'Add_10'
RDotNet.Closure
  [cse 'GetObjectType' 'I'
RDotNet.IntegerVector
  [cse 'GetObjectType' 'se'
RDotNet.SymbolicExpression[]
  [cse 'GetObjectType' 'res'
RDotNet.IntegerVector
Ready 10 0 UNI NUM
```

Creating an Executing a user-defined function in R with an array argument and result

In this example the user-defined R function will return a vector of values based upon arguments provided by APL+Win. Because the C# 'for{...}' control structure is used, a CSE script is created and run using the CSE 'Exec' method. The R-function 'runif' is used to generate n sample values of the uniform distribution over the interval [min, max].

$Z \leftarrow \text{RUserDefinedFunctionArrayResult } X; S; N; MI; MX$

⊙ N : #Uniform distribution values to return

⊙ MI: Minimum value of the range of uniform distribution values

⊙ MX: Maximum value of the range of uniform distribution values

$(N \ MI \ MX) \leftarrow X$

$X \leftarrow \emptyset$

☐ cse 'ExecStmt' 'Int32 N;'

☐ cse 'SetValue' 'N' N

☐ cse 'ExecStmt' 'Int32 MI;'

☐ cse 'SetValue' 'MI' MI

☐ cse 'ExecStmt' 'Int32 MX;'

☐ cse 'SetValue' 'MX' MX

$S \leftarrow \text{'var runif = rEng.Evaluate(@\"RUNIF<-function(n,mn,mx){res = runif(n,min=mn,max=mx);return(res);}\").AsFunction();}'$

$S \leftarrow S, \text{'var nArg = rEng.CreateIntegerVector(new Int32[]\{N\});}'$

```

S←S,⊢'var mnArg = rEng.CreateIntegerVector(new Int32[] {MI});'
S←S,⊢'var mxArg = rEng.CreateIntegerVector(new Int32[] {MX});'
S←S,⊢'var se = new SymbolicExpression[] { nArg, mnArg, mxArg };'
S←S,⊢'var res = runif.Invoke(se).AsNumeric();'
S←S,⊢'double[] dRes = new double[res.Count()];'
S←S,⊢'for (Int32 I = 0;I<res.Count();I++)'
S←S,⊢'{'
S←S,⊢' dRes[I] = res[I];'
S←S,⊢'}'

S←⊃S
□cse 'Exec' S
Z←□cse 'GetValue' 'dRes'

```

Here is the CSE script which this APL+Win function creates:

```

var      runif      =      rEng.Evaluate(@"RUNIF<-function(n,mn,mx){res      =
runif(n,min=mn,max=mx);return(res);}").AsFunction();
var nArg = rEng.CreateIntegerVector(new Int32[] {N});

```

```
var mnArg = rEng.CreateIntegerVector(new Int32[] {MI});  
var mxArg = rEng.CreateIntegerVector(new Int32[] {MX});  
var se = new SymbolicExpression[] { nArg, mnArg, mxArg };  
var res = runif.Invoke(se).AsNumeric();  
double[] dRes = new double[res.Count()];  
for (Int32 I = 0; I < res.Count(); I++)  
{  
    dRes[I] = res[I];  
}
```

When the APL+Win 'RUserDefinedFunctionArrayResult' function is run three times, 10 pseudo-random values of the uniform distribution over the interval [1, 5] are provided by the R engine for each execution of the function:

The screenshot shows the APL+Win application window with the following content:

```
APL+Win - [C:\USERS\JOE.BLAZESSIBIZ\SKYDRIVE\APL2000\C...
File Edit View Objects Walk Tools Options Window Help
InitREngine
RUserDefinedFunctionArrayResult 10 1 5
2.855743237 1.289338458 3.90902786 3.810807407 4.304371495 4.615351413
2.298555356 3.090371593 2.976923549 1.643503798
RUserDefinedFunctionArrayResult 10 1 5
3.230024327 1.973448301 2.388872828 1.227629551 2.09719009 2.956828922
2.501692034 1.944717749 2.673664764 1.557734006
RUserDefinedFunctionArrayResult 10 1 5
2.606422244 1.64437766 3.511638843 1.918087821 1.806123279 4.853687125
4.542552469 1.152673747 1.478748031 2.712527575
Ready 4 0
```

Programming Styles using R, R.Net Toolkit and APL+Win

The ensemble of R, the R.Net toolkit and APL+Win supports several programming styles. The R.Net [toolkit documentation](#) describes the first three of these programming styles. For simplicity the R cos() trigonometric function used, even though it is available in APL+Win and APL+Win merely displays the values obtained from R. In a production application R functions which are not available or convenient in C# or APL+Win would be used and the results obtained from R would be further manipulated by C# or APL+Win.

In the examples in this section it is important to note the methods by which APL+Win values are assigned to R.Net and R variables and analogously how the values of R.Net and R variables are assigned to APL+Win variables.

R variables are associated with symbols (e.g. text variable names). R variables have simple types analogous to vectors (rank 1) and matrices (rank 2).

The R.Net toolkit for R provides .Net object types such as Function, NumericVector, NumericMatrix (rank 2), CharacterVector, CharacterMatrix (rank 2), which correspond to the R variable types. The R.Net tool kit for R also provides methods to get and set the value of R variables such as `CreateNumericVector(double[])`, `GetSymbol(string).AsNumeric()`, `SetSymbol(string, NumericVector)`.

The R.Net object types can be coerced into arrays of .Net value types such as `double[]`, `double[,]`, `bool[]`. For example the R.Net NumericVector can be converted in C# to a `double[]` using C# generic extension methods, i.e. `NumericVector.ToArray<double>()`.

The APL+Win `□cse` system function 'GetValue' and 'SetValue' methods can be used to get and set the value of .Net variables that have been derived from R.Net variables using APL+Win variable values.

R.Net style #1

This style uses R expressions to perform calculations and prepare results exclusively in R. The advantage of this style is that R sample code can generally be used directly.

The APL+Win 'RNetStyle1' function illustrates this style:

```
RNetStyle1;x;y
```

```
⌈⌋APLNext 20131229
```

```
:TRY
```

```
'Style #1 - Do as much as possible in R'
```

```
□cse 'ExecStmt' 'rEng.Evaluate(@ "x <- (0:12) * pi / 12");'
```

```
⌈⌋ ↑ Create the R symbol 'x' containing the values at which
```

```
⌈⌋ the function will be evaluated
```

```
□cse 'ExecStmt' 'rEng.Evaluate(@ "y <- cos(x)");'
```

```
⌈⌋ ↑ Evaluate the cos() function at desired values and
```

```
⌈⌋ assign the results to the R symbol 'y'
```

```
x←□cse 'GetValue' 'rEng.Evaluate("x").AsNumeric().ToArray<double>()';
```

```
y←□cse 'GetValue' 'rEng.Evaluate("y").AsNumeric().ToArray<double>()';
```

```
x,[1.5]y
```

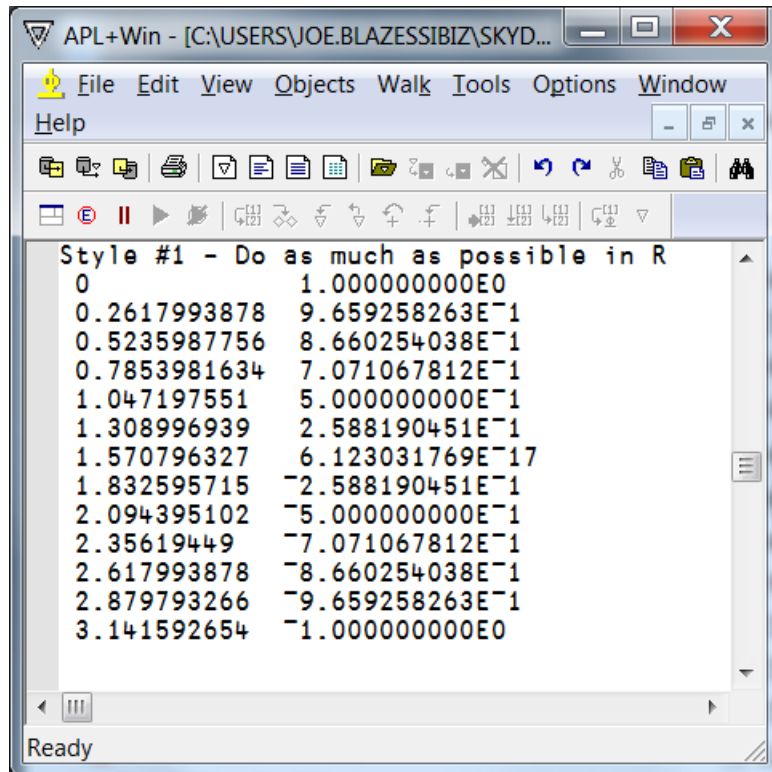
```
⌈⌋ ↑ Get the R-calculated values into APL+Win
```

```
:CATCH
```

```
'RNetStyle1: ', ☐ dm
```

```
:ENDTRY
```

When this function is executed, the results are available in APL+Win



The screenshot shows the APL+Win application window. The title bar reads "APL+Win - [C:\USERS\JOE.BLAZESSIBIZ\SKYD...". The menu bar includes "File", "Edit", "View", "Objects", "Walk", "Tools", "Options", and "Window". Below the menu bar is a "Help" button and a toolbar with various icons. The main text area displays the following text:

```
Style #1 - Do as much as possible in R
0      1.000000000E0
0.2617993878  9.659258263E-1
0.5235987756  8.660254038E-1
0.7853981634  7.071067812E-1
1.047197551   5.000000000E-1
1.308996939   2.588190451E-1
1.570796327   6.123031769E-17
1.832595715   -2.588190451E-1
2.094395102   -5.000000000E-1
2.35619449    -7.071067812E-1
2.617993878   -8.660254038E-1
2.879793266   -9.659258263E-1
3.141592654   -1.000000000E0
```

The status bar at the bottom left shows "Ready".

R.Net Style #2

This style uses R expressions to perform calculations and prepare results which can only be done in R and otherwise uses C# expressions supported by the R.Net toolkit for R whenever that is more convenient or familiar.

The APL+Win 'RNetStyle2' function illustrates this style:

```
RNetStyle2;x;y
```

```
⌈⌋APLNext 20131229
```

```
:TRY
```

'Style #2 - Mostly R Expressions, but use C# whenever convenient or familiar'

```
□cse 'ExecStmt' 'var x = rEng.Evaluate(@"x <- (0:12) * pi / 12").AsNumeric();'
```

⌈⌋ ↑ Create the C# variable x containing the values at which the function will

⌈⌋ be evaluated. The variable x has R.Net.NumericVector type.

```
□cse 'ExecStmt' 'rEng.SetSymbol("x", x);'
```

⌈⌋ ↑ Set the value of the R symbol "x" from the value of the R.Net C# variable x

```
□cse 'ExecStmt' 'var y = rEng.Evaluate("cos(x)").AsNumeric();'
```

⌈⌋ ↑ Create the R.Net C# variable 'y' containing the results of the cos() function

⌈⌋ at the desired values. The variable x has R.Net.NumericVector type.

```
x←□cse 'GetValue' 'x.ToArray<double>()';'
```

```
y←□cse 'GetValue' 'y.ToArray<double>()';'
```

```
x,[1.5]y
```

```
⌈↑ Get the R-calculated values into APL+Win
```

```
:CATCH
```

```
'RNetStyle2: ',⎕dm
```

```
:ENDTRY
```

When the APL+Win 'RNetStyle2' function is executed the same results as the APL+Win 'RNetStyle1' function are produced.

R.Net Style #3

This style increases the abstraction of R syntax using more of the R.Net toolkit features. This style has the advantage that the resulting C# methods can be re-used and composed with other methods in the same .Net project. This style also continues to use C# whenever it is more convenient or familiar.

The APL+Win 'RNetStyle3' function illustrates this style:

```
RNetStyle3;x;y
```

```
⌈⌋APLNext 20131229
```

```
:TRY
```

```
'Style #3 - C# Abstraction of R syntax using the R.Net toolkit'
```

```
□cse 'ExecStmt' 'var x = rEng.CreateNumericVector(Enumerable.Range(0, 13).Select(i => i * Math.PI / 12).ToArray());'
```

⌈⌋ ↑ Create the C# variable (R.Net.NumericVector type) x containing the values at which the function will be evaluated.

```
□cse 'ExecStmt' 'var cos = rEng.GetSymbol("cos").AsFunction();'
```

⌈⌋ ↑ Create the C# variable (R.Net.Function type) cos which encapsulates the R cos() function.

```
□cse 'ExecStmt' 'var y = cos.Invoke(new[] { x }).AsNumeric();'
```

⌈⌋ ↑ Create the C# variable (R.Net.NumericVector type) containing the results of the evaluation by using the

⌈⌋ R.Net.Invoke() method on the R.Net.Function variable cos.

```
x←⊞cse 'GetValue' 'x.ToArray<double>()';  
y←⊞cse 'GetValue' 'y.ToArray<double>()';  
x,[1.5]y  
⊞ ↑Get the R-calculated values into APL+Win
```

```
:CATCH  
'RNetStyle3: ',⊞dm  
:ENDTRY
```

When the APL+Win 'RNetStyle3' function is executed the same results as the APL+Win 'RNetStyle1' or 'RNetStyle2' functions are produced.

R.Net and APL+Win Style #4

This programming style is similar to style #3 except that APL+Win is used whenever it is more convenient or familiar.

The APL+Win 'RNetAndAPLStyle4' function illustrates this style:

```
RNetAndAPLStyle4;x;y
```

```
⌈⌋APLNext 20131231
```

```
⌈⌋io←1
```

```
:TRY
```

'Style #4 - Use APL+Win whenever more convenient or familiar'

```
⌈⌋cse 'ExecStmt' 'double[] dV;'
```

```
x←o(¯1+ι13)÷12 ⌈⌋Use APL+Win to generate the required values
```

```
⌈⌋cse 'SetValue' 'dV' x ⌈⌋Set the C# variable dV using the APL+Win values
```

```
⌈⌋cse 'ExecStmt' 'var x = rEng.CreateNumericVector(dV);'
```

```
⌈⌋ ↑ Create the C# variable (R.Net.NumericVector type) x containing the values  
at which the function will be evaluated.
```

```
⌈⌋cse 'ExecStmt' 'var cos = rEng.GetSymbol("cos").AsFunction();'
```

```
⌈⌋ ↑ Create the C# variable (R.Net.Function type) cos which encapsulates the R  
cos() function.
```

```
y←⌈⌋cse 'GetValue' 'cos.Invoke(new[] { x }).AsNumeric().ToArray<double>()';
```

⌈↑ Get the R-calculated values into APL+Win using the R.Net.Invoke() method on the R.Net.Function variable cos.

x,[1.5]y ⌈ Display or use the values in APL+Win

:CATCH

'RNetStyle4: ',⎕dm

:ENDTRY

When this function is executed the same results are obtained as the functions illustrating the other styles.

Utility functions in the APL+Win 'R Stat& Graph.w3' workspace

The APL+Win 'R Stat&Graph.w3' workspace contains the APL+Win 'Plot' function which makes 2-D R-plots easy by separating the generation of values from the mechanics of creating an R-plot.

```
Plot X;xyVals;xLAB;yLAB;mainLAB
```

```
⊞ xyVals[;1]: x-axis values
```

```
⊞ xyVals[;2]: y-axis values
```

```
⊞ xLAB      : text x-axis label
```

```
⊞ yLAB      : text y-axis label
```

```
⊞ mainLAB   : chart title
```

```
(xyVals xLAB yLAB mainLAB)←X
```

```
X←⍬
```

```
sink←⍬cse 'ExecStmt' 'string chartFnm = @"chartFnm.bmp";'
```

```
sink←⍬cse 'ExecStmt' 'File.Delete(chartFnm);'
```

```
sink←⍬cse
```

```
'ExecStmt'
```

```
'rEng.SetSymbol("chartFnm",rEng.CreateCharacterVector(new
string[]{chartFnm}));'
```

```
sink←□cse 'ExecStmt' 'rEng.Evaluate("bmp(chartFnm)");'
```

⦿ ↑Set the saved chart bitmap destination

```
sink←□cse 'ExecStmt' 'double[,] xyVals = new double[,]{};'
```

```
sink←□cse 'SetValue' 'xyVals' xyVals
```

```
sink←□cse
```

'ExecStmt'

```
'rEng.SetSymbol("xyVals",rEng.CreateNumericMatrix(xyVals));'
```

```
sink←□cse 'ExecStmt' 'string xLAB = "";'
```

```
sink←□cse 'SetValue' 'xLAB' xLAB
```

```
sink←□cse
```

'ExecStmt'

```
'rEng.SetSymbol("xLAB",rEng.CreateCharacterVector(new string[]{xLAB}));'
```

```
sink←□cse 'ExecStmt' 'string yLAB = "";'
```

```
sink←□cse 'SetValue' 'yLAB' yLAB
```

```
sink←□cse
```

'ExecStmt'

```

'rEng.SetSymbol("yLAB",rEng.CreateCharacterVector(new string[] {yLAB}));'

sink←□cse 'ExecStmt' 'string mainLAB = "";'
sink←□cse 'SetValue' 'mainLAB' mainLAB
sink←□cse 'ExecStmt'
'rEng.SetSymbol("mainLAB",rEng.CreateCharacterVector(new
string[] {mainLAB}));'

sink←□cse 'ExecStmt' 'rEng.Evaluate(@ "plot(xyVals[,c(1)],xyVals[,c(2)], col =
""darkred"", xlab=xLAB, ylab=yLAB, main=mainLAB)");'
sink←□cse 'ExecStmt' 'rEng.Evaluate(@ "dev.off()");'

F←'F'□wi 'Create' 'Form' ('size' 40 80) ('caption' 'R-plot in APL+Win Form')
P←'F.P'□wi 'Create' 'Picture' ('where' 0 0 40 80) ('size' 30 60) ('style' 0)
P□wi 'bitmap' 'chartFnm.bmp'
sink←F□wi 'Wait'

```

The APL+Win 'Gauss' and 'Unif' functions can be used to generate pseudo-random samples from the normal and uniform probability distributions respectively.

```
Z←Gauss X;n;m;s;sink
```

⌈ X[1]: #estimates desired

⌈ X[2]: mean of Gauss distribution

⌈ X[3]: standard deviation of Gauss distribution

⌈ Z : Vector of estimates

```
(n m s)←X
```

```
sink←□cse 'ExecStmt' 'double mGauss = 0;'
```

```
sink←□cse 'SetValue' 'mGauss' m
```

```
sink←□cse 'ExecStmt'
```

```
'rEng.SetSymbol("mGauss",rEng.CreateNumericVector(new  
double[] {mGauss}));'
```

```
sink←□cse 'ExecStmt' 'double sGauss = 0;'
```

```
sink←□cse 'SetValue' 'sGauss' s
sink←□cse 'ExecStmt'
'rEng.SetSymbol("sGauss",rEng.CreateNumericVector(new double[] {sGauss}));'

sink←□cse 'ExecStmt' 'Int32 nGauss = 0;'
sink←□cse 'SetValue' 'nGauss' n
sink←□cse 'ExecStmt'
'rEng.SetSymbol("nGauss",rEng.CreateIntegerVector(new Int32[] {nGauss}));'

Z←□cse 'GetValue'
'rEng.Evaluate("rnorm(nGauss,mGauss,sGauss)").AsNumeric().Take(nGauss).To
Array();'
```

$Z \leftarrow \text{Unif } X; n; \text{max}; \text{min}; \text{sink}$

⊙ $X[1]$: #estimates desired

⊙ $X[2]$: minimum value of the range of estimates

⊙ $X[3]$: maximum value of the range of estimates

⊙ Z : Vector of estimates

$(n \text{ min max}) \leftarrow X$

$\text{sink} \leftarrow \square \text{cse 'ExecStmt' 'Int32[] nUnif = new Int32[1];'}$

$\text{sink} \leftarrow \square \text{cse 'SetValue' 'nUnif[0]' n}$

$\text{sink} \leftarrow \square \text{cse 'ExecStmt'}$

$\text{'rEng.SetSymbol("nUnif", rEng.CreateIntegerVector(nUnif));'}$

$\text{sink} \leftarrow \square \text{cse 'ExecStmt' 'double[] minUnif = new double[1];'}$

$\text{sink} \leftarrow \square \text{cse 'SetValue' 'minUnif[0]' min}$

$\text{sink} \leftarrow \square \text{cse 'ExecStmt'}$

$\text{'rEng.SetSymbol("minUnif", rEng.CreateNumericVector(minUnif));'}$

$\text{sink} \leftarrow \square \text{cse 'ExecStmt' 'double[] maxUnif = new double[1];'}$

```
sink←□cse 'SetValue' 'maxUnif[0]' max  
sink←□cse 'ExecStmt'  
'rEng.SetSymbol("maxUnif",rEng.CreateNumericVector(maxUnif));'  
  
Z←□cse 'GetValue' 'rEng.Evaluate("runif(nUnif, min=minUnif, max =  
maxUnif)").AsNumeric().Take((Int32)(nUnif[0])).ToArray()';
```

R For Actuaries

A few interesting links about the use of R in actuarial mathematics:

- <http://toolkit.pbworks.com/f/R%20Examples%20for%20Actuaries%20v0.1-1.pdf>
- <http://toolkit.pbworks.com/w/page/22358245/R%20Examples%20For%20Actuaries>
- <http://www.r-bloggers.com/sampling-for-monte-carlo-simulations-with-r/>
- <http://www.springer.com/statistics/computational+statistics/book/978-1-4419-1575-7>

Resources

- [APL2000 Consulting Services](#)
- [R-Project.org](#)
- [Comprehensive R Archive Network](#)
- [R.Net](#)
- [Beta distribution in R](#)
 -
- [Rclr](#)
- Some examples:
 - <http://psychwire.wordpress.com/2011/06/25/importing-and-displaying-a-data-frame-with-c-and-r-net/>
 - <http://www.codeproject.com/Articles/25819/The-R-Statistical-Language-and-C-NET-Foundations>
 - <http://msenux.redwoods.edu/math/R/normal.php>
 - http://www.ats.ucla.edu/stat/r/library/lecture_graphing_r.htm

- <http://rtutorialseries.blogspot.com>
- <http://www.stat.berkeley.edu/classes/s133/saving.html>
- <https://github.com/jmp75/rdotnet-onboarding>
- <http://csg.sph.umich.edu/docs/R/graphics-1.pdf>
- Bing or Google: “plotting in R stat”